1 An arithmetic progression has tenth term 11.1 and fiftieth term 7.1. Find the first term and the common difference. Find also the sum of the first fifty terms of the progression.

2 Jill has 3 daughters and no sons. They are generation 1 of Jill's descendants.
Each of her daughters has 3 daughters and no sons. Jill's 9 granddaughters are generation 2 of her descendants. Each of her granddaughters has 3 daughters and no sons; they are descendant generation 3.

Jill decides to investigate what would happen if this pattern continues, with each descendant having 3 daughters and no sons.
(i) How many of Jill's descendants would there be in generation 8 ?
(ii) How many of Jill's descendants would there be altogether in the first 15 generations?
(iii) After $n$ generations, Jill would have over a million descendants altogether. Show that $n$ satisfies the inequality

$$
n>\frac{\log _{10} 2000003}{\log _{10} 3}-1
$$

Hence find the least possible value of $n$.
(iv) How many fewer descendants would Jill have altogether in 15 generations if instead of having 3 daughters, she and each subsequent descendant has 2 daughters?

3 (i) Find $\sum_{r=1}^{5} \frac{21}{r+2}$.
(ii) A sequence is defined by

$$
\begin{aligned}
u_{1} & =a, \text { where } a \text { is an unknown constant, } \\
u_{n+1} & =u_{n}+5 .
\end{aligned}
$$

Find, in terms of $a$, the tenth term and the sum of the first ten terms of this sequence.

4 The second term of a geometric progression is 24 . The sum to infinity of this progression is 150 . Write down two equations in $a$ and $r$, where $a$ is the first term and $r$ is the common ratio. Solve your equations to find the possible values of $a$ and $r$.
$5 S$ is the sum to infinity of a geometric progression with first term $a$ and common ratio $r$.
(i) Another geometric progression has first term $2 a$ and common ratio $r$. Express the sum to infinity of this progression in terms of $S$.
(ii) A third geometric progression has first term $a$ and common ratio $r^{2}$. Express, in its simplest form, the sum to infinity of this progression in terms of $S$ and $r$.

6 Find the second and third terms in the sequence given by

$$
\begin{aligned}
& u_{1}=5 \\
& u_{n+1}=u_{n}+3 .
\end{aligned}
$$

Find also the sum of the first 50 terms of this sequence.

7 A geometric progression has first term $a$ and common ratio $r$. The second term is 6 and the sum to infinity is 25 .
(i) Write down two equations in $a$ and $r$. Show that one possible value of $a$ is 10 and find the other possible value of $a$. Write down the corresponding values of $r$.
(ii) Show that the ratio of the $n$th terms of the two geometric progressions found in part (i) can be written as $2^{n-2}: 3^{n-2}$.

